



---

# Multipath and Atmospheric Propagation Errors in Offshore Aviation DGPS Positioning

**J. Paul Collins, Peter J. Stewart  
and Richard B. Langley**

2nd Workshop on Offshore Aviation Research  
Centre for Cold Ocean Resources Engineering  
Memorial University of Newfoundland  
St. John's, Nfld.

September 23–24, 1998

---

*Geodetic Research Laboratory, Department of Geodesy and Geomatics Engineering, University of New Brunswick.*



# INTRODUCTION

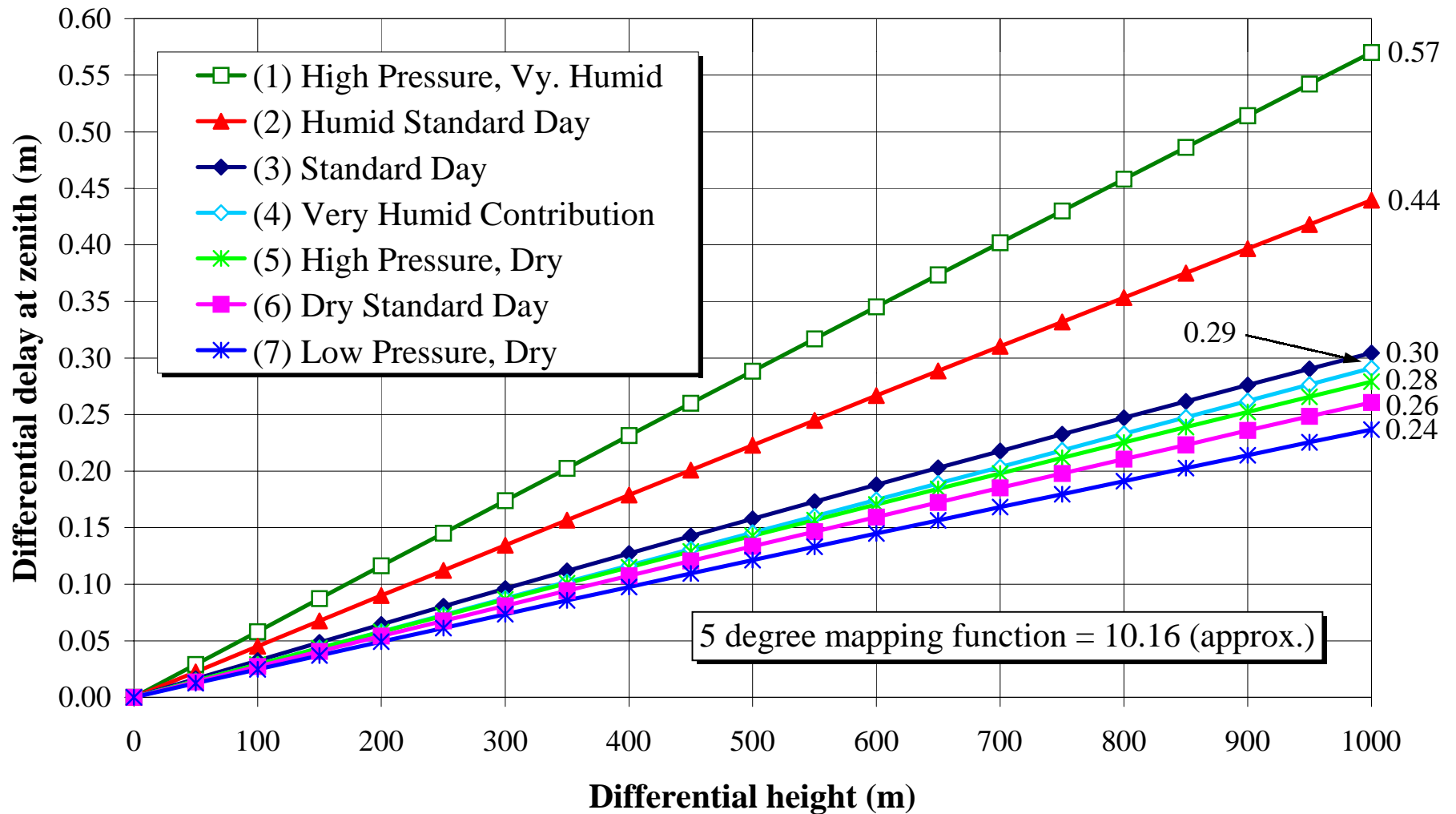
---



- Part 1:
  - Impact of tropospheric delay on DGPS pseudoranges.
  - Results of using simple model to account for vertical separation of aircraft and reference antennas.
- Part 2:
  - Impact of reference station multipath on computed aircraft position.
  - Possible solutions, software and hardware techniques.

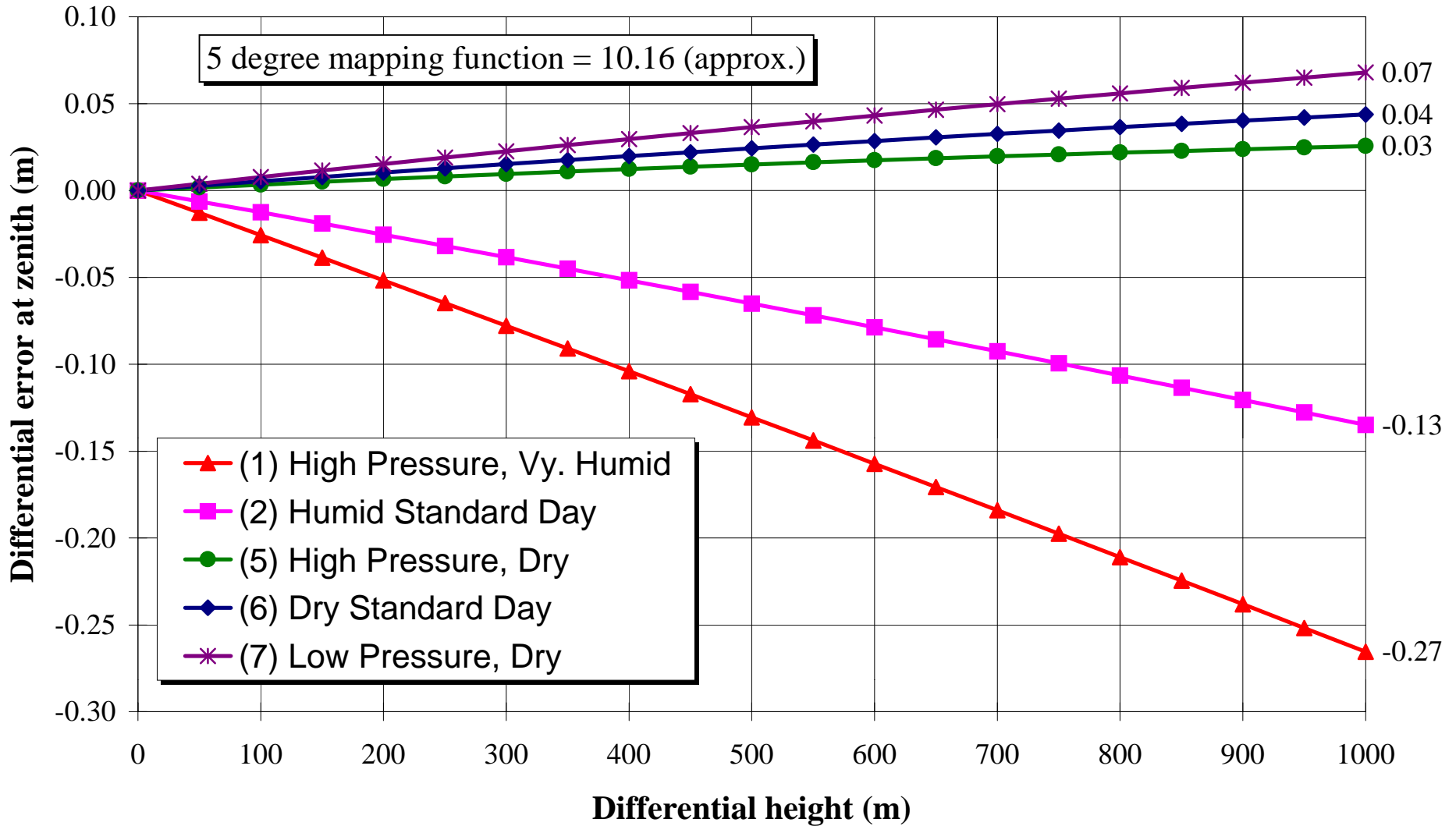


## Differential tropospheric zenith delay upto 1000m above reference station. (Represents zenith DGPS correction error due to altitude separation.)

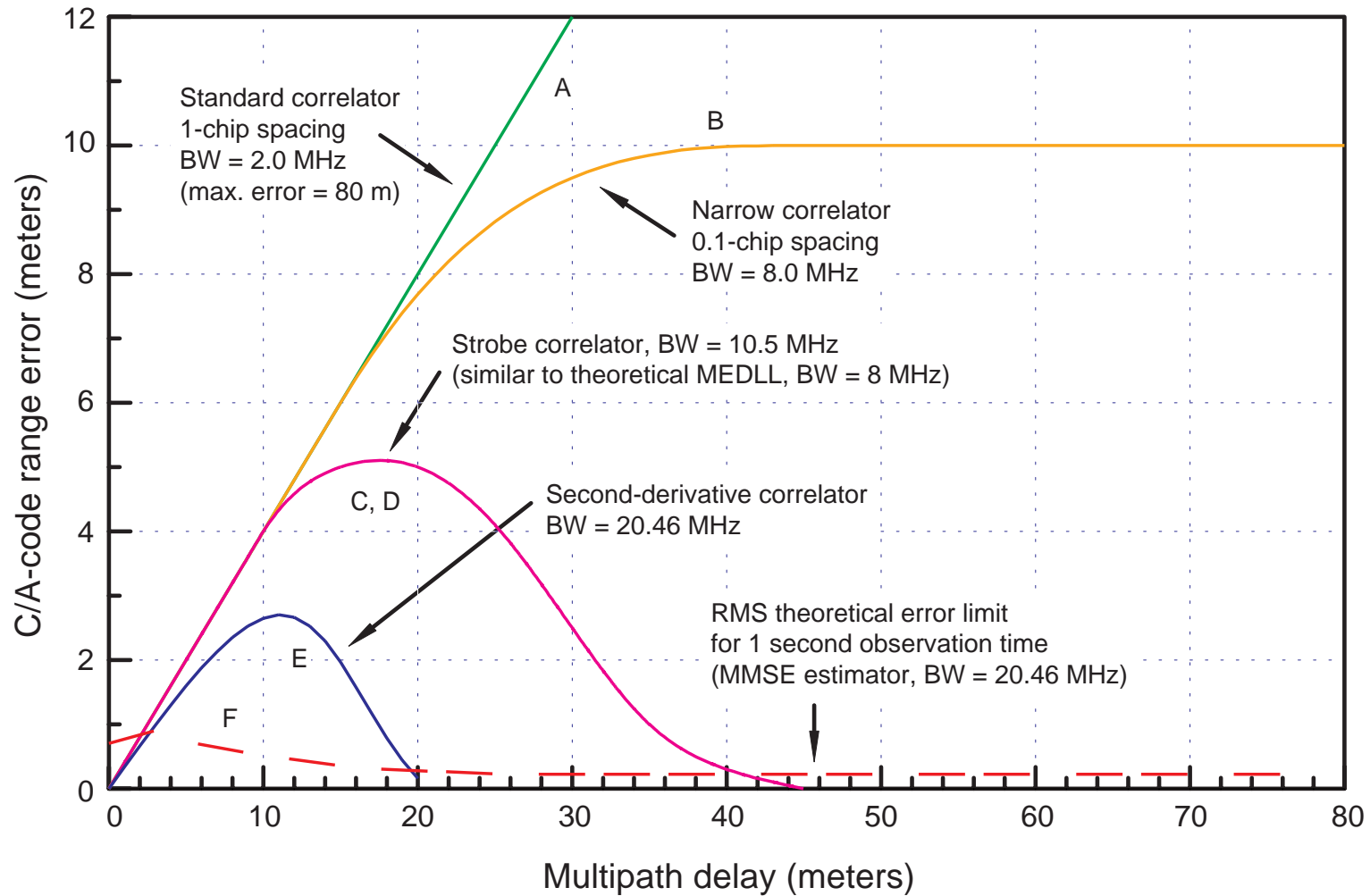




# DGPS correction errors at the zenith, when using UNB1 tropospheric delay model at aircraft and reference station.



# RECEIVER TECHNOLOGY



Weill, L.R. (1997). "Conquering multipath: The GPS accuracy battle." *GPS World*, April, pp. 59-66.



## MULTIPATH MODELLING

---

Requires pseudorange and dual frequency carrier phase measurements:

$$C_1 = \rho + c(dT - dt) + I_1 + T + m_{C_1} + n_{C_1}$$

$$\Phi_1 = \rho + c(dT - dt) + \lambda_1 N_1 - I_1 + T + m_{\Phi_1} + n_{\Phi_1}$$

$$\Phi_2 = \rho + c(dT - dt) + \lambda_2 N_2 - I_2 + T + m_{\Phi_2} + n_{\Phi_2}$$

Single frequency combination includes ionospheric contribution:

$$C_1 - \Phi_1 = 2I_1 - \lambda_1 N_1 + m_{C_1} + n_{C_1} - m_{\Phi_1} - n_{\Phi_1}$$

$$I_2 = \alpha I_1; \quad \alpha = \left( \frac{f_1}{f_2} \right)^2$$

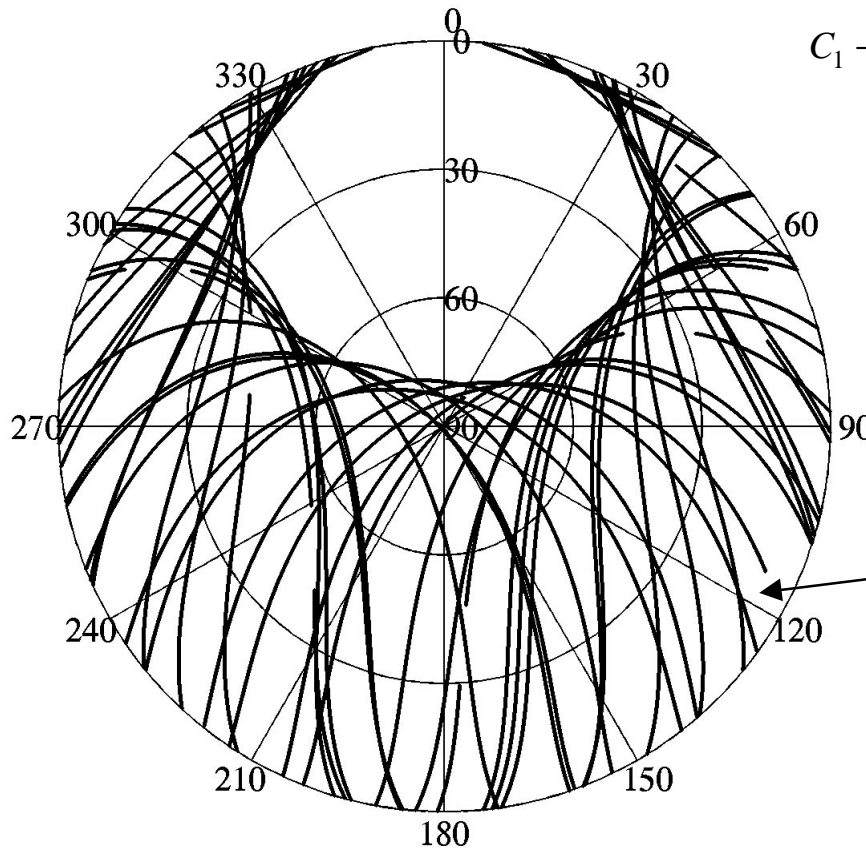
$$2 \frac{(\Phi_1 - \Phi_2)}{(\alpha - 1)} = 2I_1 + 2 \frac{(\lambda_1 N_1 - \lambda_2 N_2)}{(\alpha - 1)} + 2 \frac{(m_{\Phi_1} - m_{\Phi_2})}{(\alpha - 1)} + 2 \frac{(n_{\Phi_1} - n_{\Phi_2})}{(\alpha - 1)}$$

$$C_1 - \left( 1 + \frac{2}{\alpha - 1} \right) \Phi_1 + \left( \frac{2}{\alpha - 1} \right) \Phi_2 = m_{C_1} + n_{C_1} + B + M_{\Phi} + N_{\Phi}$$

Final combination dominated by pseudorange multipath ( $m_{C_1}$ ) and noise ( $n_{C_1}$ ).

---

# CALIBRATING MULTIPATH



$$C_1 - 4.0915\Phi_1 + 3.0915\Phi_2 = m_{C_1} + n_{C_1} + B + M_\Phi + N_\Phi$$

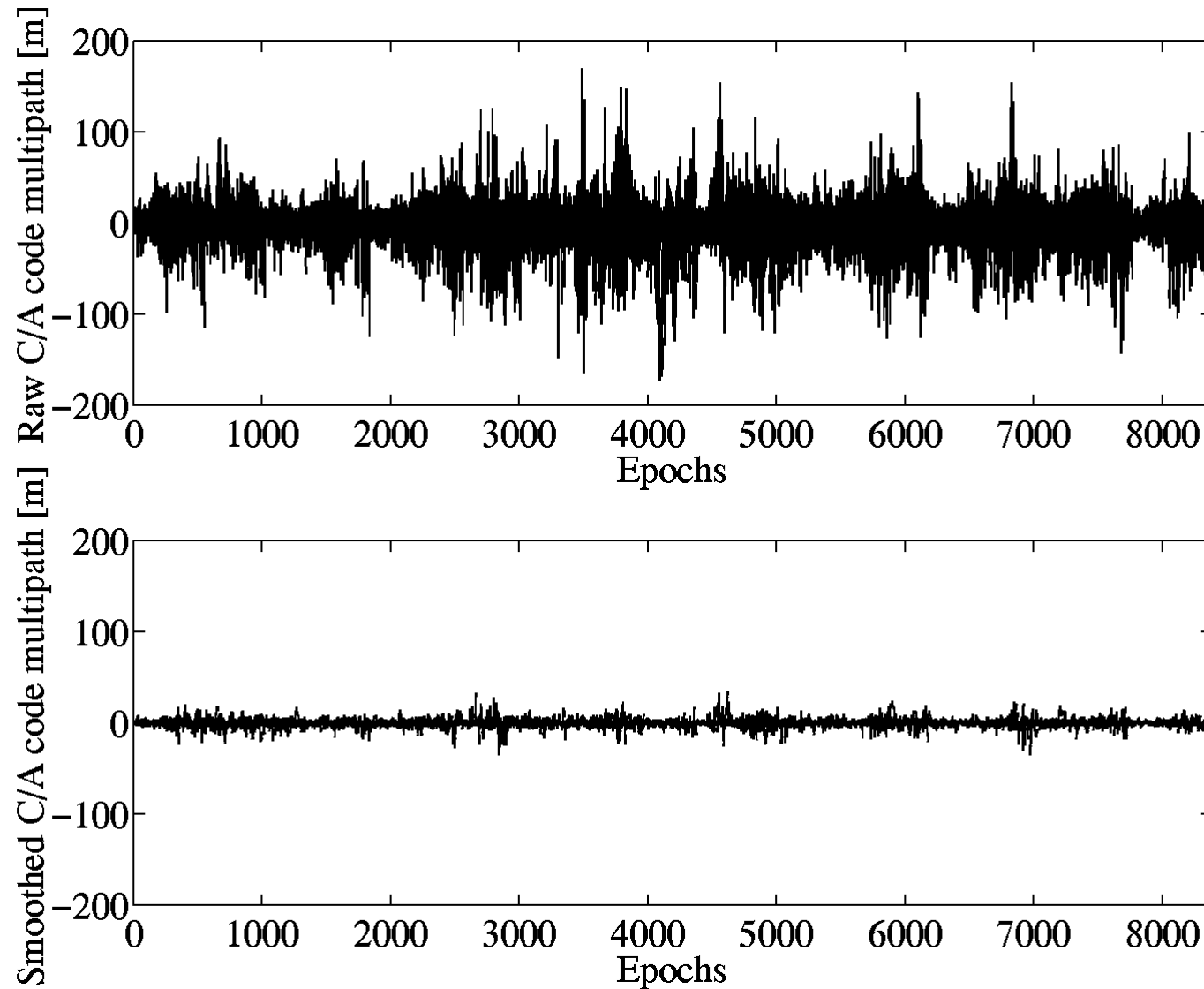
Combination of pseudorange ( $C_1$ ) and dual frequency carrier phases ( $\Phi_1, \Phi_2$ ) is dominated by pseudorange multipath ( $m_{C_1}$ ) and noise ( $n_{C_1}$ ). However, accuracy is limited by unknown biases,  $B$ , primarily the combination of the carrier phase integer ambiguities.

This technique calibrates  $B$  from repeated multipath measurements at satellite cross-over points, where the multipath should be the same for both satellites. Multipath ‘maps’ can be constructed as a function of azimuth and elevation angle.

Kee, C. and B. Parkinson (1994). “Calibration of multipath errors on GPS pseudorange measurements.”  
*Proceedings of ION GPS-94*, Salt Lake City, Utah, September 20-23, pp. 353-363.



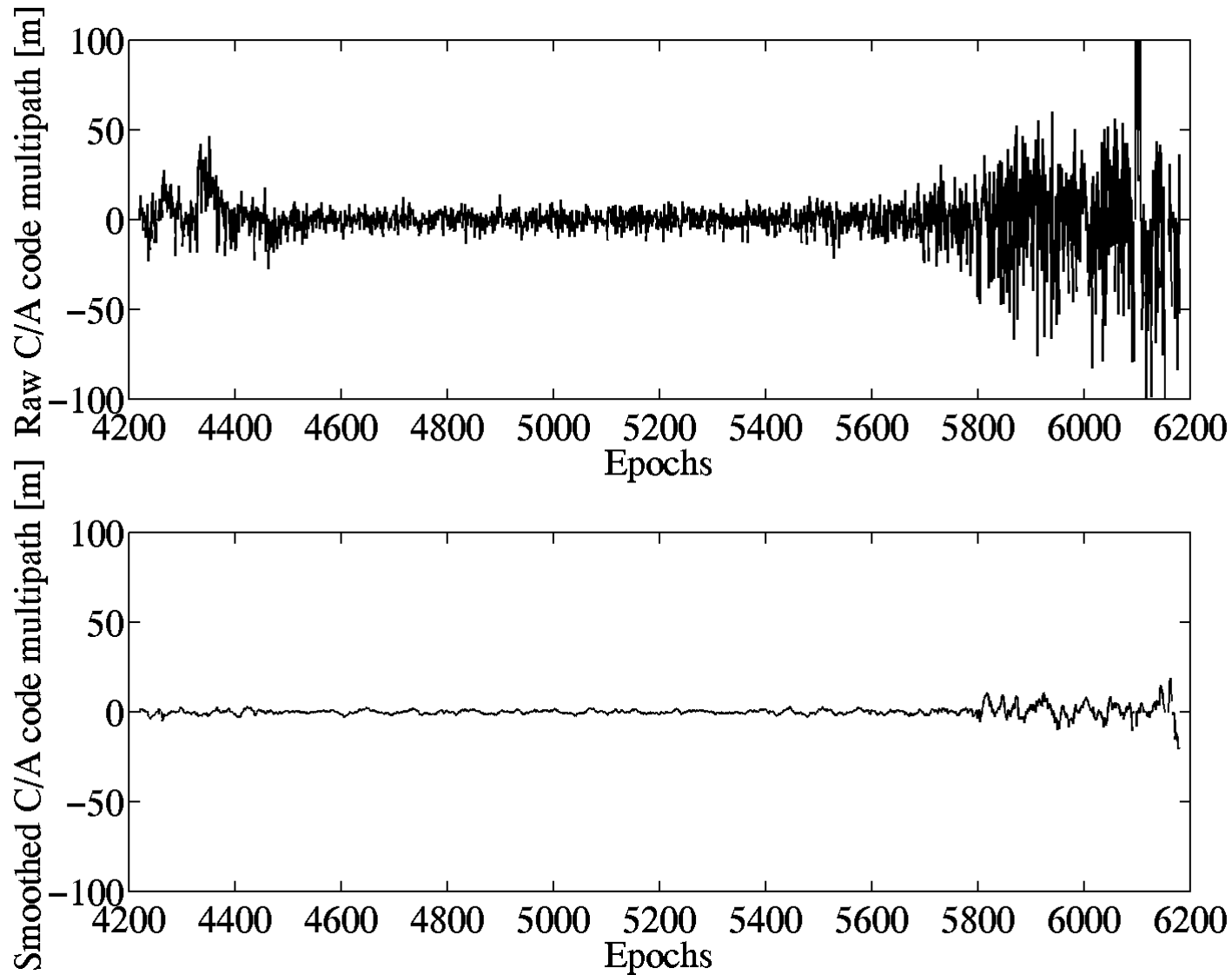
## RAW AND SMOOTHED C/A CODE MULTIPATH (1)





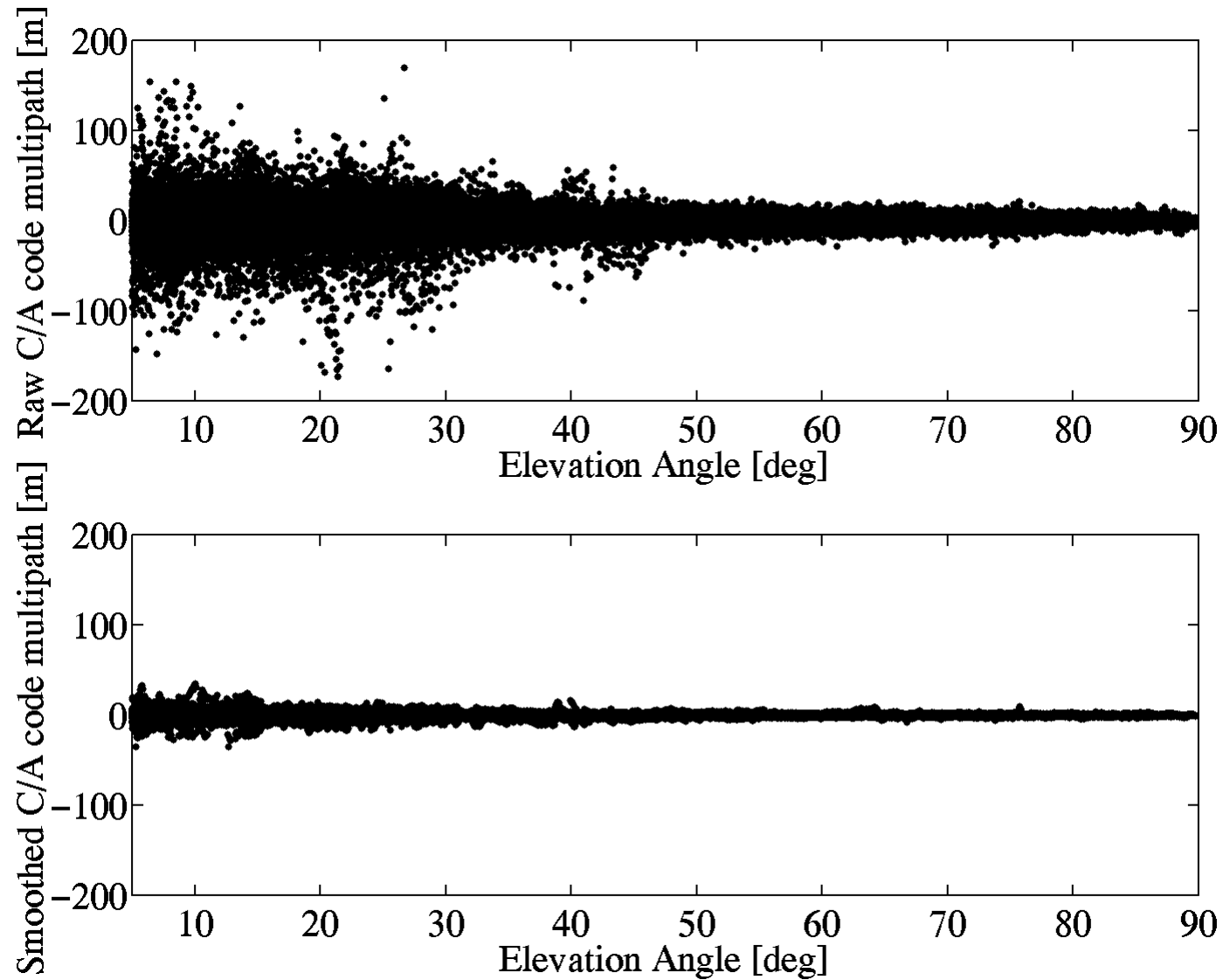


## RAW AND SMOOTHED C/A CODE MULTIPATH (2)



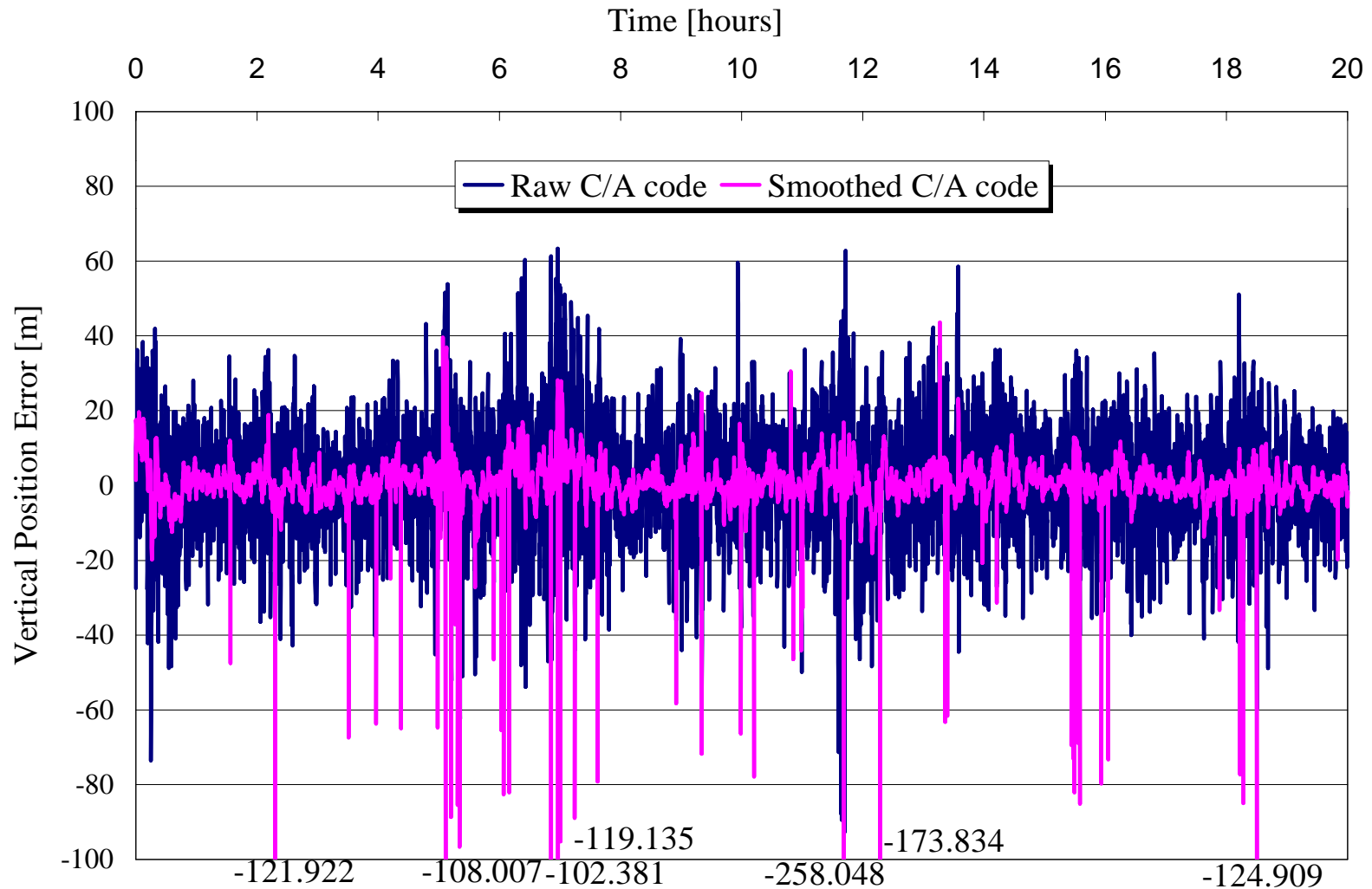


# MULTIPATH ELEVATION ANGLE DEPENDENCE



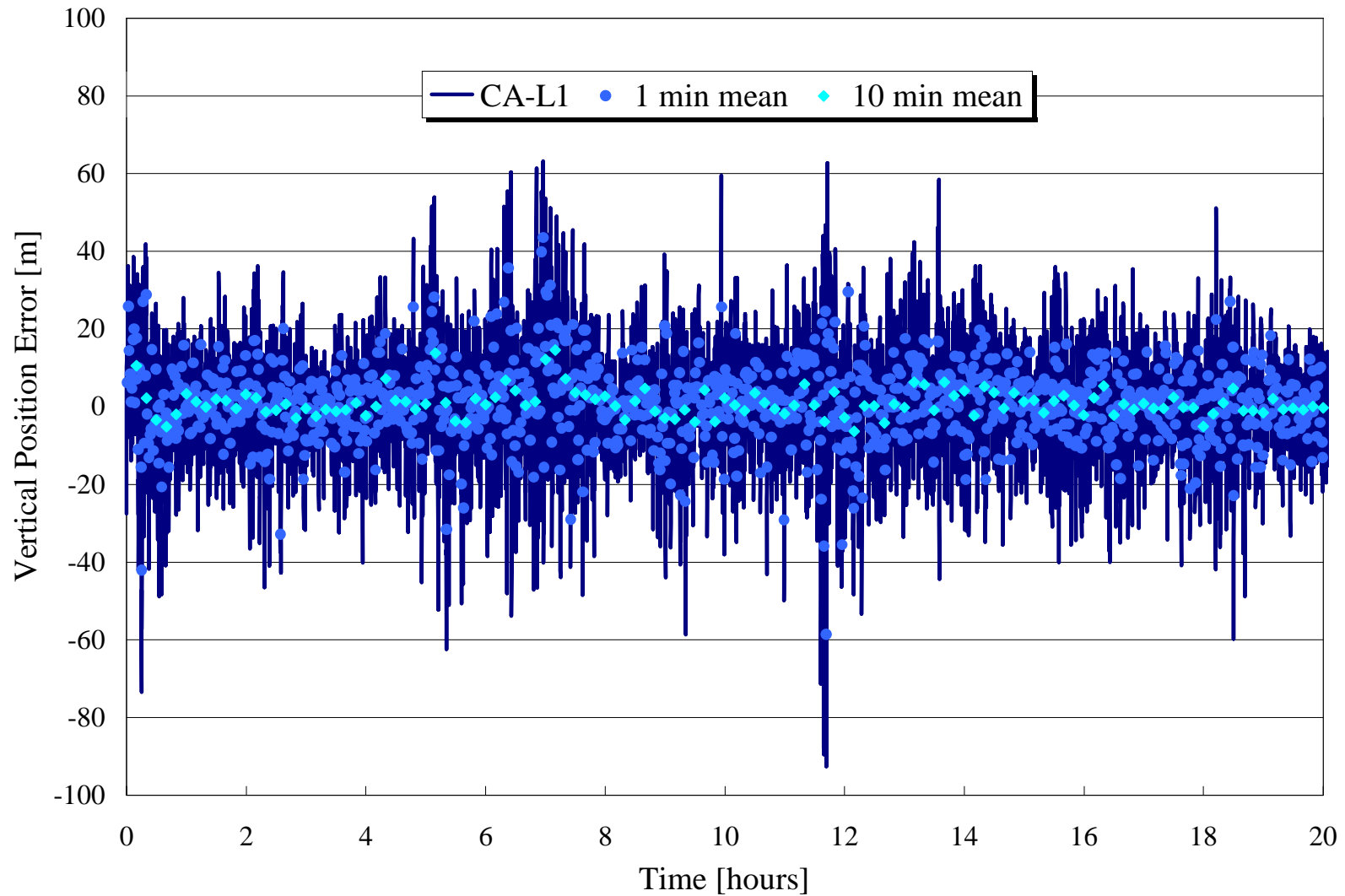


## RAW AND SMOOTHED DATA, VERTICAL POSITION





# RAW DATA, SMOOTHED POSITIONS





## RESULTS SUMMARY

---



- Residual tropospheric effects, after adequate modelling, only contribute sub-decimetre biases in height.
- Error in height due to multipath could approach 100 metres.
- Smoothed data susceptible to cycle slips in noisy reference station environment.
- Filtering aircraft positions using velocity information should reduce large errors.



## CONCLUSIONS

---



- Residual tropospheric delays should not be a problem for offshore aviation DGPS.
  - Simple model drastically reduces what small error there is.
- Multipath has potential for severe problems.
  - Combination of techniques:
    - Receiver and antenna technology to limit maximum multipath error.
    - Filtering in either pseudorange domain and/or position domain at aircraft using velocity information.